

A two-dimensional reaction-advection-diffusion model of the spread of fire in wildlands

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Abstract

The aim of this research is to develop a model of the spread of wildfires that is computationally efficient and easy-to-use, yet comprehensive enough to capture the major phenomena that govern the behaviour of a real fire. Namely, the pyrolysis of wood; the combustion of a mono-phase medium composed of premixed gas of fuel and air; the heat transferred by diffusion, convection and radiation considering emission and absorption of hot semi-transparent gases; and the thermal energy transport due to atmospheric wind and spatial distribution of vegetation. The model consists of two coupled partial differential equations, one representing the mass formation of each chemical species involved in the combustion, and the other ensuring the balance of enthalpy. The dimensionality reduction sought by modelling these three-dimensional (3D) phenomena in two-dimensional (2D) space is an intricate problem that has been overcome by means of pseudo-3D terms in the energy balance equation. For instance, the convection in the direction perpendicular to the 2D domain of the model has been represented as heat loss whose magnitude is linearly dependent on the temperature difference between the ambient and the simulation domain. Thus, the pseudo-3D convection term acts as a sink of thermal energy. It is important to note, however, that some environment properties have necessarily been disregarded in the interest of efficiency. Thus, the effect of topography on the spread of fire has been ignored in this model. In addition, the balance of momentum in the simulation plane is not included in the formulation as air density is considered independent of temperature and the wind velocity field is steady-state and uniform. Furthermore, the diffusion coefficient is augmented to account for the energy transport due to convection inside the flattened vegetal substrate, which is abstractly represented as a pre-mixed gaseous layer. This augmentation has been calibrated for particular environment conditions such as the porosity of the fuel and its spatial distribution so that the model can be used as a tool for prediction of fire propagation. Making use of the 4th-Order Runge-Kutta method and running simulations for different constraints and boundary-initial conditions, results appear realistic. The presented fire-spread model is aimed at supporting the design of innovative fire management and suppression technologies and strategies, as well as to function as a decision-support tool to assist fire fighters in the use of current technology. Hence it must be both realistic and computationally efficient. Nonetheless, a more advanced 3D high-fidelity model is currently under development at the other end of the spectrum of the accuracy/efficiency trade-off with the aim to provide better insight into the fire dynamics.

Keywords: wildfire propagation, modelling, reaction, advection, diffusion, fuel, combustion, radiation, suppression.

1. Introduction

Modelling wild fires is a real challenge because of its complex combination of several interdependent phenomena acting at different length scales. Few researchers have attempted

to handle this cumbersome problem. According to the methodologies utilised, the different fire models can be grouped in classes. Based on the mathematical formulation adopted, models can be classified as either *continuous* or *cellular automata* based (Sullivan, 2009, p.349; Sullivan, 2009, p.369; Papadopoulos and Pavlidou, 2010; Séro-Guillaume et al., 2008). The first group consists of models based on the laws of physics, with mathematical formulations in terms of coupled partial differential equations typically including balances of mass, momentum and energy. Instead, the cellular automata approach models the domain as a set of nodes that can have only a discrete number of states – e.g. unburnt, burning or burnt. In (Anez et al., 2017), a multilayer cellular automaton was used to model smouldering using three layers: the fuel (ash, char, dry fuel, wet fuel), the heat layer (heat release, no heat, heat losses), and oxygen (oxygen or nitrogen). This allowed a far more detailed estimation of the fire dynamics compared with the simpler burnt/burning/unburnt scheme. The evolution in time of the automata is determined by probabilistic transition laws that involve the state of the neighbouring nodes. The advantage of the cellular automata approach over the physics-based one is its considerably faster computation.

One of the most eminent continuous models of wildfire that can be found in the literature was developed by members of the *Laboratoire d'Energetique et de Mechanique Theorique et Appliquee* (LEMTA) (Séro-Guillaume and Margerit, 2002; Margerit and Séro-Guillaume, 2002). It is a three-dimensional (3D) multiphase and multiscale wildfire model which elegantly depicts the fire phenomena from the smallest to the largest scale. In fact, they believe the repertoire of fire models should be classified according to the length-scale to be investigated: *microscopic* scale, where vaporisation and pyrolysis of the solid fuel are the main involved phenomena; *mesoscopic* scale, at which the geometry of the vegetation (leaves, branches, etc.) heavily affects the heat fluxes from solid to surrounding air; *macroscopic* scale, where the combustion occurs; and *gigascopeic* scale, where the fire is driven by atmospheric wind and topography. A way to overcome this complexity and modelling at large scales in order to have a faster simulation is upscaling through averaging and by the convenient use of Large Eddy Simulation (LES) for turbulence modelling. But one of the most severe limitations of large-scale models are the errors associated with point-to-point comparison, which is critical given that the rate of spread is very sensitive to small variations (Houssami et al., 2018).

Furthermore, the available freeware simulators of wildfire can also be differentiated between continuous and cellular automata based models. The most well known simulators world-wide are FARSITE (Finney, 1998), Prometheus (Tymstra et al., 2010) and the Fire Dynamics Simulator (FDS) (McGrattan and Forney, 2004; McGrattan, 2006). The first two are based on the same Huygens principle for the determination of the fire front perimeter, which consists of the envelope contour of ellipses whose focuses are located in the previous step's fire-front, and whose shapes depend on many environmental parameters (e.g. wind) and fuel properties (e.g. moisture level). These fire simulators are mostly focused on determining the fire spread efficiently in order to assist fire management operations. On the other hand, FDS is more focused on capturing as many detailed features of fire phenomena as possible. It can be both 2D and 3D and makes use of the direct physics approach. Séro-Guillaume et al. (Séro-Guillaume et al., 2008) acknowledge two main types of continuous approaches to modelling fire. The one adopted by Margerit et al. (Margerit and Séro-Guillaume, 2002) simplifies and averages from the most complex and detailed mathematical formulation to the most practical one that can be more easily implemented numerically. Conversely, the FDS approach starts from the simplest 3D gaseous-phase

combustion model and adds complexity through the development of several *submodels* that are superposed to the main simulation and interact with it – e.g. volume-less Lagrangian particles (McGrattan, 2006) used to model solid firebrand particles floating in the air and exchanging mass, momentum and energy with the fluid while reacting with it. These submodels usually have mostly empirical bases, stemming from extensive and expensive experimental observations. Some recent submodels either developed or under development are as follows:

- Correlation between the firebrand generation and the fire behaviour in order to determine fluxes, sizes and separation distances (Thomas et al., 2017, p. 864-871).
- Development of smouldering models (combustion of solid microporous media), both numerical (Anez et al., 2017) and empirical ones.
- Wildland-urban interface Fire Dynamics Simulator (WFDS), which is an extension of the American National Institute of Standards and Technology's (NIST) FDS.
- Regarding upscaling techniques: determining the heat transfer coefficient between solid and fluid phases at macroscopic level using a surrogate model based on numerical experiments of the heat transfer throughout a fractal model of vegetation geometry (Collin and Lamorlette, 2012).
- Radiation, which is a very complex problem, especially if the whole spectrum is considered.
- Incomplete combustion models (mostly empirical) due to variation of oxygen flux (Thomas et al., 2017, p.855-863).

There is extensive debate upon which fire modelling approach is the best in capturing its dynamics. For instance, Papadopoulos (Papadopoulos and Pavlidou, 2010) states that FARISTE “is considered to be the most precise fire propagation simulation model by most of the researchers around the world”, whilst Sullivan (Sullivan, 2009) claims that still FARSITE and Prometheus are the best simulators found in literature that can reproduce historical fires. At the same time, there are other research centres that focus their attention on the direct physics approach, proudly acclaiming its rigour in detecting the fire dynamics. For example, FDS is the result of 25 years of collaboration between many researchers across the world, whilst LEMTA's fire-spread models have been developed during 15 years of work. In line with (Séro-Guillaume et al., 2008), we are interested in classifying fire models according to their purpose, for instance to achieve a fast (possibly real-time) prediction or to capture some microscale phenomena.

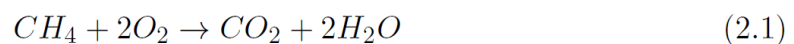
The aim of this research is to model the spread of forest fire efficiently in order to support the design of innovative fire management and suppression technologies and strategies, while also comprising a decision-support tool to assist fire-fighters in their use of current technology. Therefore, the model must be at the same time efficient and comprehensive enough to capture the major phenomena that govern the behaviour of a real fire.

The proposed fire-spread model is given by a 2D reaction-advection-diffusion equation that describes the combustion of a mono-phase medium composed of premixed gas of fuel and air. It can be placed in the 2D direct-physics semi-empirical reaction-diffusion class of fire spread models, and it is similar to the Ferragut's (Ferragut et al., 2007) and Margerit's

(Margerit and Séro-Guillaume, 2002) 2D models. By reducing dimensionality, some phenomena of fire dynamics are disregarded, e.g. the buoyancy due to density changes of the medium immersed in a gravitational field. The energy transport due to atmospheric wind is modelled, though the wind field is limited at this stage to be steady-state and uniform throughout the 2D space considered. The effect of the slope and that of the water vapour pressure are left to be accounted for in a 3D model that is currently being developed. Another simplifying assumption is that 2D convection is negligible, which is reasonable since the velocities induced by density variation in the horizontal plane are very small, with the resulting energy transport comprising less than 1% of the total energy fluxes. Considering that buoyancy is not modelled and assuming that the chemical reaction rate depends mostly on temperature and mole fractions of fuel and oxygen, the density variation due to temperature changes has no strong effect on the fire dynamics modelled. Hence density is assumed to be constant, and the momentum balance and mass conservation are not formulated. Thus, the mixed gases are confined within their original location, just as if pyrolysis gasses were to be burnt exactly where they had been released. The diffusion coefficient is corrected in this efficient model in order to account for the energy transport due to 2D convection inside the premixed layer – i.e. in the vegetation stratum. Furthermore, two pseudo-3D terms are added into the energy balance equation with the intention of modelling the energy losses due to convection and radiation in the direction perpendicular to the 2D domain being modelled (vertical direction). Horizontal radiation is modelled so as to affect only the neighbouring cells, since the cell size in the discretised domain can be set larger than the optical thickness or radiation absorption length. The heat capacity at constant pressure of each chemical species is considered to be constant and equal to an average value in the considered temperature range, from $T_{\text{amb}} = 293$ K (ambient temperature) to approximately 1200 K (maximum temperature). Although, in the eventuality of strong wind, the temperature may rise to peaks of 1500K.

2. The 2D Wildfire Spread Model

The considered irreversible chemical reaction in (2.1) represents the combustion of the pyrolysis gasses in air, which is composed of oxygen, carbon dioxide, vapour and nitrogen.



The fire-spread model can be represented by a system of five coupled partial differential equations, namely the enthalpy balance in (2.2) and the four equations in (2.3) for the consumption or formation of each chemical species (*Fuel*, *O₂*, *CO₂*, *H₂O*), i.e. $j = 1, \dots, 4$.

$$\frac{\partial T}{\partial t} = F_T(T, X_j) \quad (2.2)$$

$$\frac{\partial X_j}{\partial t} = F_{X_j}(T, X_j) \quad (2.3)$$

Equation (2.2) is expanded in (2.4) where the phenomenon modelled by each term is clearly labelled, namely: 1) the *combustion energy* term including the combustion enthalpy (h_c) and the reaction rate; 2) the *transport* term accounting for atmospheric wind; 3) the *diffusion* terms; 4) the *pseudo-3D convection* term accounting for energy loss by vertical convection; the *2D radiation* terms; and the *pseudo-3D radiation* term modelling vertical emission.

$$\rho c_p \frac{\partial T}{\partial t} = \underbrace{-\rho h_c \frac{M}{M_1} r}_{\text{Diffusion}} - \underbrace{\rho c_p u_i^* \frac{\partial T}{\partial x_i}}_{\text{Transport}} + \dots$$

$$\underbrace{k \frac{\partial}{\partial x_i} \left(\frac{1}{c_p} \frac{\partial c_p T}{\partial x_i} \right) + k \frac{\partial}{\partial x_i} \left(\frac{1}{c_p} \frac{\partial h_c T}{\partial x_i} \right)}_{\text{Convection}} + \dots \quad (2.4)$$

$$\underbrace{C_a (T_{\text{amb}} - T)}_{\text{2D-Radiation}} + \dots$$

$$\underbrace{\sigma \varepsilon \left[4 dx_i \frac{\partial}{\partial x_i} \left(T^3 \frac{\partial T}{\partial x_i} \right) \right]}_{\text{2D-Radiation}} + \underbrace{\sigma \varepsilon \left[\frac{T_{\text{amb}}^4 - T^4}{dx_3} \right]}_{\text{pseudo3D-Radiation}}$$

$$\frac{\partial X_i}{\partial t} = -\frac{\theta_i}{\theta_{fuel}} \frac{M}{M_{fuel}} r \quad ; \quad \text{with } i = 1, \dots, 4 \quad (2.5)$$

In order to close the system composed by (2.4) and (2.5), additional closure equations are required, in particular for:

- The molar mass of the mixture (M) in (2.6), which is the weighted summation of each chemical species molar mass (M_i) by their mass fractions (X_i).
- The constant pressure heat capacity of the mixture (c_p) in (2.7), which is the weighted summation of all the partial heat capacities (c_{pi}).
- The combustion rate (r) following the Arrhenius law in (2.8), where the subscripts ‘1’ stands for *fuel* and ‘2’ for *oxygen*. The formulation is the empirical formula related to wood pyrolysis in (Ragland et al., 1991). Bear in mind the pre-exponential coefficient (A_r) for following discussion.
- The specific combustion enthalpy (h_c) in (2.9), which is the summation of all the formation enthalpies at the local temperature (T).

$$M = \sum_{i=1}^5 X_i M_i \quad (2.6)$$

$$c_p = \sum_{i=1}^5 X_i \frac{M_i}{M} c_{pi} \quad (2.7)$$

$$r(T, X_1, X_2) = -\delta_{(T, X_{1,2})}^+ A_r T X_1^{0.5} X_2 \exp\left(-\frac{T_a}{T}\right) \quad (2.8)$$

$$h_c = \frac{H_c(T)}{M} = -\frac{1}{M} \sum_{i=1}^5 \theta_i H_i(T) = \frac{1}{M} \sum_{i=1}^5 \theta_i (H_{i,\text{ref}} + M_i c_{pi} (T_{\text{ref}} - T)) \quad (2.9)$$

The conductivity (k), the pre-exponential coefficient (A_r) and the optical absorption length (dx_i) have been calibrated (see *Table 2*) using the results obtained by FARSITE simulator (Finney, 1998), not having any experimental data available at the moment. The representative values considered are the burnt area, radius, and the maximum temperature. Given that the burning (a.k.a. flaming) area can be smaller than the burnt area, the latter has been chosen for calibration purposes as the flaming area is very dynamic and its estimation affected by the numerical model used.

For instance, we performed two exemplar calibrations for two types of fuels structurally different: the values in *Table 2* have been obtained for the fuel model FM3 (tall coarse grass) and FM10 (coniferous trees) (Scott and Burgan, 2005). More precisely, FM10 consists of 15m trees with 4m base, whose canopy coverage has been set to 100% in the presented simulations, with a density of $0.2 \text{ kg}\cdot\text{m}^{-3}$. Moreover, the selected elevation is 300 m and the moisture level about 20%. The remaining known parameters and some characteristic variables are listed in *Table 1*.

Please note that the optical absorption length, for radiation modelling, has to be smaller than or equal to the cell size in order for the model to be valid. Moreover, the asymptotic wind magnitude, above the vegetation stratum, has to be reduced in order to take the drag into account. Hence the modified wind velocity (u_i^*) in (2.4) is obtained by multiplying the wind velocity by a reduction coefficient (w_r), which is a function of the fuel type and of the canopy coverage. The higher the canopy coverage and the denser the fuel type, the smaller the reduction coefficient. For instance, by our calculations during calibration phase, 10 m/s for FM10 corresponds to approximately $1.3 \times 10^{-3} \text{ m/s}$ in the premixed gas layer.

3. Results and Discussion

The simulations have been performed on a $100\text{m} \times 100\text{m}$ domain, and their results appear realistic from both qualitative and quantitative point of views. However, in order to use this simulation tool for prediction of fire propagation, the parameters of the model must be calibrated for particular environmental conditions, including fuel properties and spatial distribution.

<i>Symbol</i>	<i>Description</i>	<i>Value</i>	<i>Units</i>
R	Universal gas constant	8.314	$\text{J}\cdot\text{mol}^{-1}\cdot\text{K}^{-1}$
$T_{\text{amb}}(T_{\text{ref}})$	Ambient (reference) temperature	298.15	K
T_{ig}	Ignition temperature	573	K
T_a	Activation temperature	684	K
$P_{\text{amb}}(P_{\text{ref}})$	Ambient (reference) pressure	101325	Pa
ρ	Gas mixture density	1.2172	$\text{kg}\cdot\text{m}^{-3}$
A_r	Pre-exponential coefficient (Arrhenius)	(*)	-
C_a	Turbulent convection coefficient in atmosphere	0.065	$\text{J}\cdot\text{m}^{-3}\cdot\text{K}^{-1}\cdot\text{s}^{-1}$
k	Thermal conductivity	(*)	$\text{W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$

c_p	Specific heat capacity at constant pressure	calculated	$\text{J}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$
X_f	Initial fuel molar fraction	0.1	-
σ	Stefan-Boltzmann constant	$5.6704\text{e-}8$	$\text{W}\cdot\text{m}^{-2}\cdot\text{K}^{-4}$
ε	Emissivity factory (< 1)	0.55	-
dx_i	Optical absorption length	(*)	M
dx_3	Optical absorption length in z direction	1	M
h_c	Specific combustion enthalpy	calculated	$\text{J}\cdot\text{kg}^{-1}$
w_r	Wind reduction coefficient	(*)	-
Δt	Time step	7.5	S
$\Delta x = \Delta y$	Cell-size	1	M

Table 1 – General settings for simulation of fire spread with fuel model FM10. (* calibrated parameters)

Symbol	FM3	FM10	Units
k	$5.5703\text{e-}01$	$6.3750\text{e-}02$	$\text{W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$
A_r	$4.1699\text{e-}05$	$6.6250\text{e-}06$	-
dx_i	0.4	0.1	m
w_r	$7.5106\text{e-}5$	$1.3075\text{e-}04$	-

Table 2 – Values of parameters describing the fuel model FM3 and FM10.

Figure 1.a shows the classical *ring-shaped* flame front, which has been used for calibration purposes, spreading radially from the ignition points at the same rate for uniformly distributed fuel and no wind. In case of both single and multiple ignition points and zero wind condition, the estimation error of the burnt area (with respect to FARSITE simulation) is less than 1%.

In turn, Figure 1.b shows the energising effect of wind: the flame front is distorted, the area affected by the fire is enlarged, and the maximum temperature increases (from 1215 K to about 1297 K in this case). The presence of wind results in a ‘teardrop’ shape of the fuel consumption due to the asymmetric spread of the fire, as can be observed in Figure 2.b. In presence of wind and with single/multiple ignition points, the estimation error of the burnt area oscillates between less than 1% to approximately 30% (for very intense wind of up to 80 m/s speed). The stronger the wind, the larger the discrepancies between FARSITE simulations and the presented model simulations. It is hard to assess whether one or the other are the most correct simulator of reality, but for sure a large part of the error is inherent to the mathematical formulation and the numerical methods that have been used, let alone the dimensionality reduction. It is interesting to note that in those regions where flames persist in the same location, for instance at zero wind condition or in particular stagnation points, the fuel mass fraction tends to zero (Figure 2.a) whereas the fuel tends to be only partially consumed in the presence of wind (Figure 2.b) as the flame is blown away from the original ignition points.

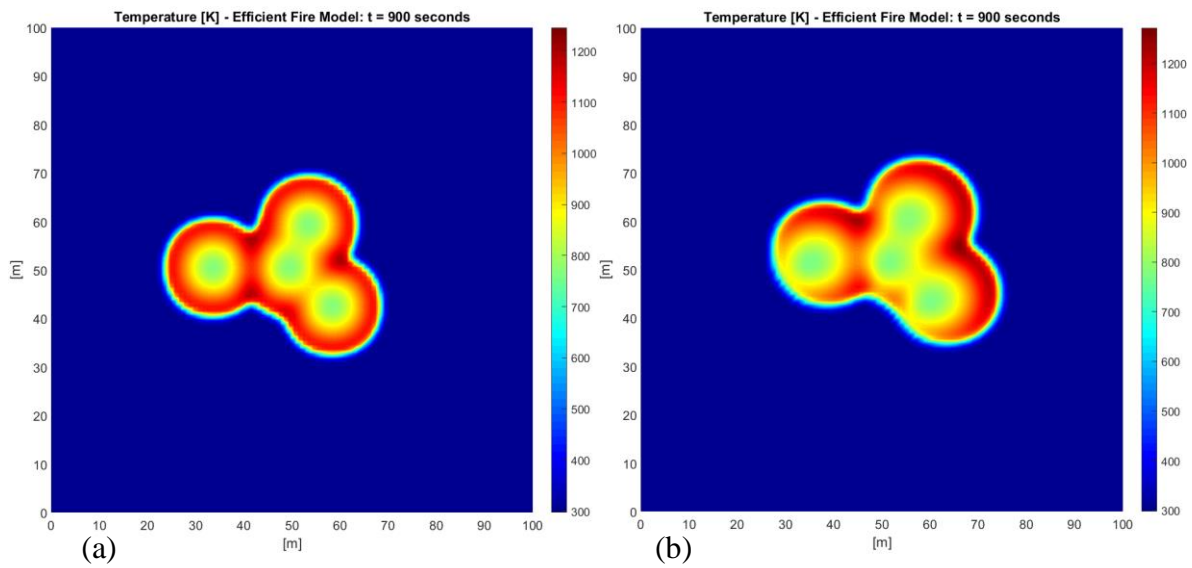


Figure 2 – Flaming Area: Temperature field at 15 min after four-points random ignition (a) without wind and (b) with strong wind of 40 m/s for FM10.

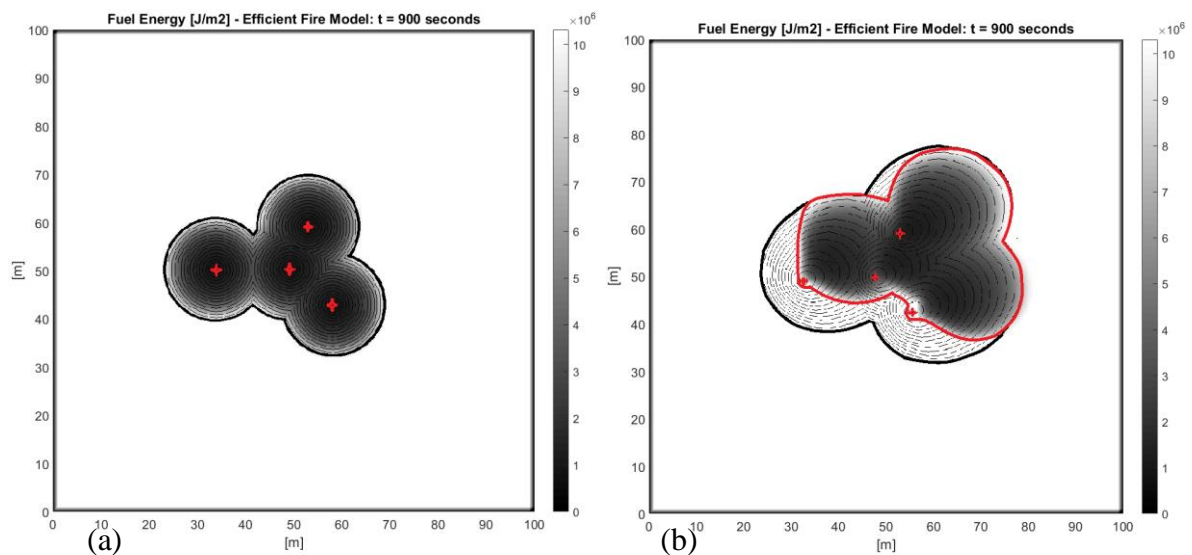


Figure 3 – Burnt Area: Distribution of fuel energy at 15 min after four-points random ignition (a) without wind and (b) with strong wind of 40 m/s for FM10. The red stars represent the ignition points (the same of Figure 1), and black areas correspond to zero-fuel condition. The thick black contour corresponds to FARSITE prediction, while the red one is obtained by the presented model.

4. Conclusion

The output of the presented research is a successful attempt to simulate efficiently and with a high level of accuracy the spread of wildfires with the use of a macroscopic two-dimensional reaction-advection-diffusion model. The developed model shows its versatility to be calibrated for any type of fuel models, tackling any environmental condition (except for topography) – e.g. moisture and wind. Thanks to its simplicity and computational lightweight (e.g. on a standard quad-core i7 computer, it predicts 1 min of fire dynamics in

approximately 1 sec computational time for 10^4 unit cells), this model has been coupled with a swarm of drones (Innocente and Grasso, 2018) in order to develop an autonomous technology to either extinguish or mitigate wildfires. The use of this robust technology aims to considerably lower the risks to human lives during firefighting operations. Thus, the presented model is both realistic and computationally efficient. Nonetheless, a more advanced and intensive 3D high-fidelity model is currently under development with the aim to provide more accurate insight into the fire dynamics.

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